

MAGNET ALIGNMENT REVISITED

Subject arose at last CM; some confusion

I have revisited this

Chris Rogers searched the literature:

Four previous studies in MICE notes 64, 77, 202, 229

Some confusion about alignment of trackers and / or spectrometer solenoids

Alignment of the trackers *cannot* affect the emittance of the beam

- but can (obviously) affect the measurement of it
- must be known well enough

Alignment of S/C magnets can affect:

- a) Performance of channel (emittance reduction)
- b) Alignment studies & commissioning studies

Previous studies concentrated on (a); I concentrate on (b)

Work almost complete, MICE note 3 / 4 written

PHYSICS OVERVIEW

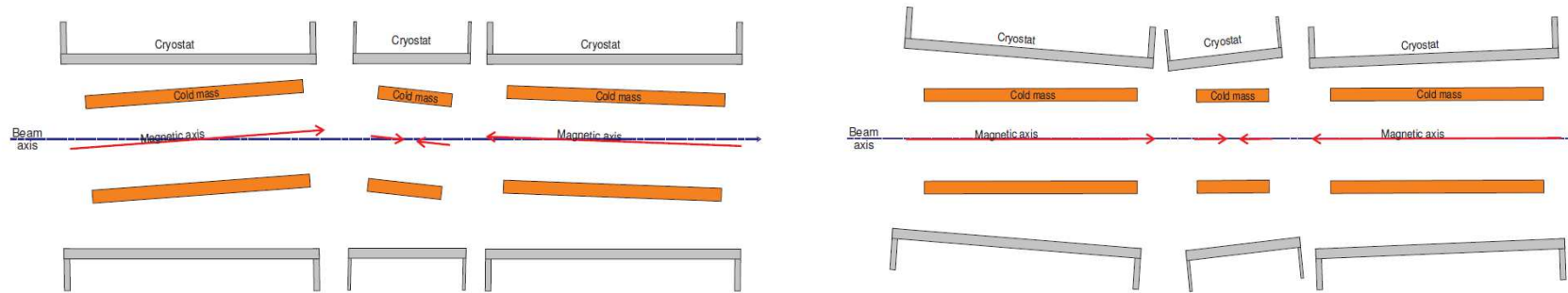


Figure 1: Misaligned modules in Step IV, much exaggerated.

Undesirable

Desirable

Modules whose magnetic axes are offset & tilted wrt beam axis will give pt kicks to muons

**Small kicks will move CoG of beam but will not change its emittance :
CoG in x , px , & c are subtrcated**

Movement of CoG of beam, especially if momentum dependent, will make alignment & commissioning v. difficult to understand.

PREVIOUS STUDIES

MICE note	Tilt ψ (mr)	Offset d (mm)	Criterion	Comment
64	< 2.4	< 1.8	Reduce 15% $\Delta\epsilon/\epsilon$ to 14%	MC study; tolerances deduced from offsetting only one coil of one FC in Step VI
77	< 6.0 (rms)	3.0 (rms)	< 0.1% systematic increase in emittance	Extensive MC study of Step VI with random offsets and tilts of coils
202	< 10	< 2	'< 1% of 10%'	MC study of Step VI; beam started in centre of upstream SS ($z = -4.7$ m) (ψ deduced as $\langle p_t \rangle / p_z = 2/200 = 0.01$)
229	< 1	< 3	1% error on $\Delta\epsilon/\epsilon$	MC study; refers to <i>tracker</i> alignment; fields not shifted (?)

Table 1: Summary of previous alignment studies. In all cases the beam was started inside the upstream spectrometer solenoid.

In all cases simulated beam started at ~ mid point of SSU

None considered what happens to a reference muon entering from outside

The alignment tolerance was derived as “2mm – 2 mr” from dEps/Eps

EXPLORE WHAT HAPPENS TO REF. MUON

Simple tracking code in magnetic field

3D field model based on B_z on axis

- gives error fields due to tilted & offset coil
- more than adequate for small tilts and paraxial muons
- details in MICE note

Fast to run so I can play with it & get feedback

→ Plenty of sanity checks

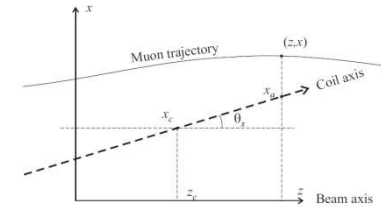


Figure 18: Geometry used for field calculation. Angles and offsets are small. z is the beam axis, θ_x is a small rotation around the y axis.

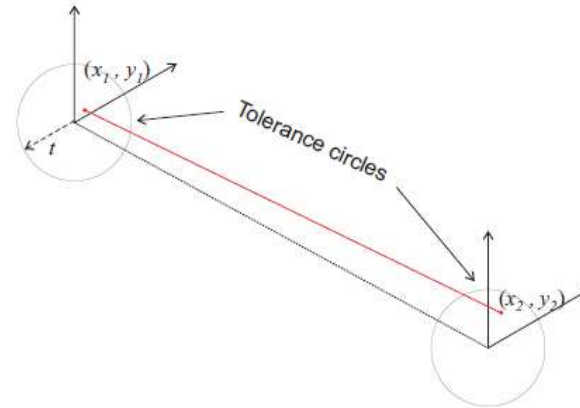
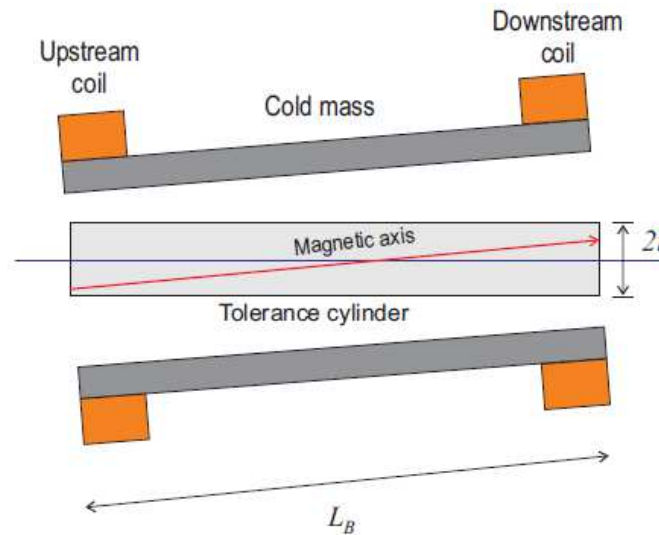
The coils are divided radially into coaxial cylindrical current sheets; all current sheets in a coil have the same tilts and offsets in x and y . In the beamline system the centre of a coil is at (x_c, y_c, z_c) where x_c and y_c are small offsets from zero. The x component of the magnetic field experienced by a muon at (x, y, z) is

$$B_x = \sum_{\text{sheets}} \left(B_z \theta_x - \frac{(x - x_a) \theta B_z}{2} \right)$$

where θ_x is a small rotation around the y axis in the $x-z$ plane and $x_a = x_c + (z - z_c)\theta_x$ is the x coordinate of the axis of the coil at z ; the geometry is sketched in figure 18.

B_z is the z component of the field on the axis of a current sheet. The sum is taken over all sheets in all coils. The first term in the expression for B_x is simply the component of the axial field of the sheet resolved in the x direction; the second follows from $\nabla \cdot \mathbf{B} = 0$.

Tolerance Definition



“x mm – y mr” definition per coil hard to interpret for coils on common bobbin

Practical definition – easy to use / give to surveyors:

Bobbin axis must lie within a t mm radius cylinder of beam axis

→ Translates to circles at ends of modules (flange faces)

Following studies use bobbins rather than individual coils

All for STEP VI 200 MeV/c Flip mode, empty channel

Aligned but offset channel:

All magnetic axes parallel but offset from beam axis by 2 mm in x

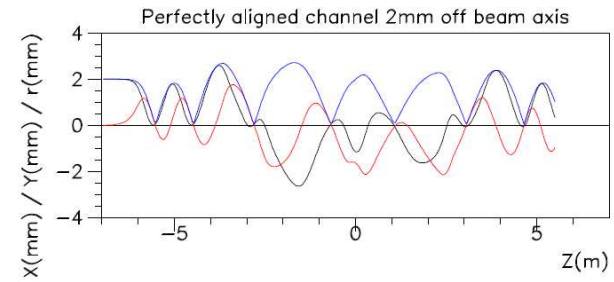
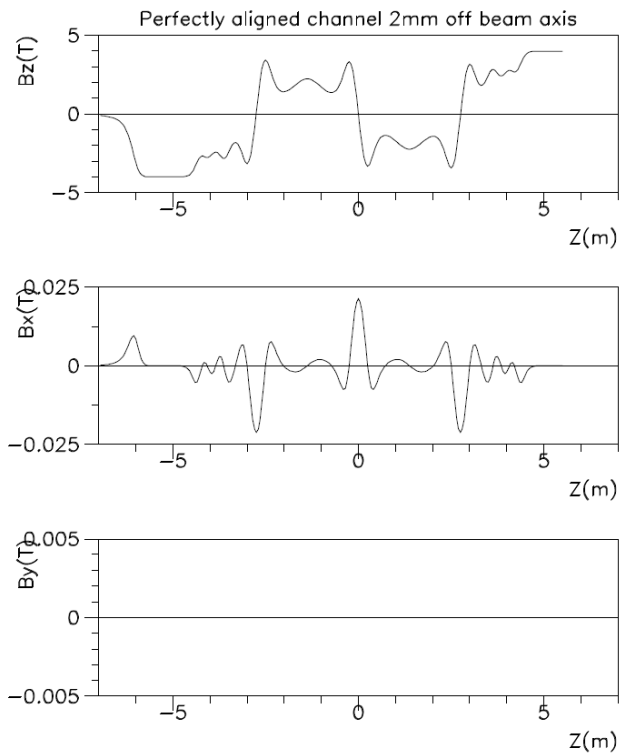
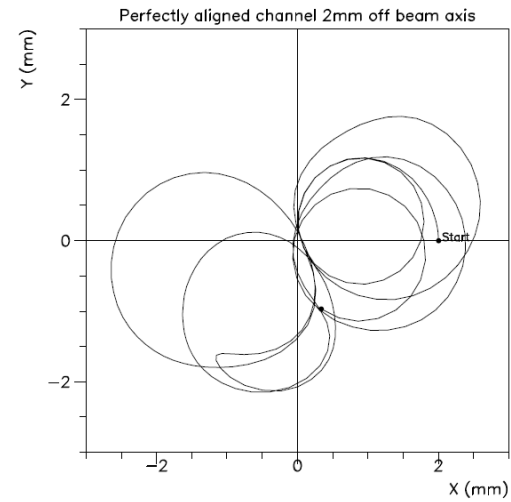


Figure 4: Trajectory of a 200 MeV/c reference muon, x - z (black), y - z (red) and r (blue), for channel axis offset by 2 mm in x .

200 MeV/c



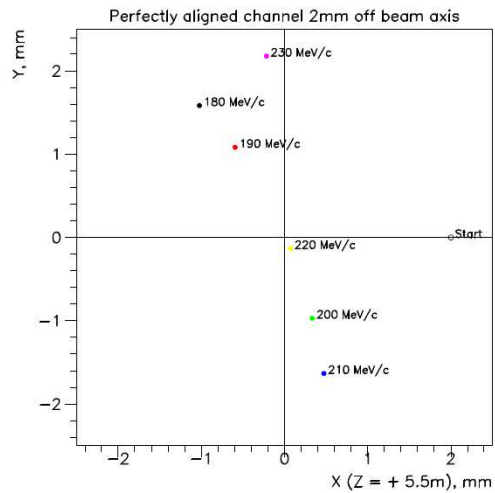
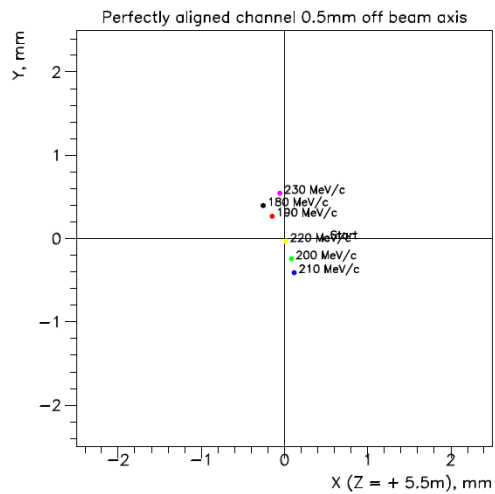


Figure 6: $x - y$ with respect to magnetic axis at $z = 5.5$ m of reference muons of different momenta for channel axis offset by 2 mm in x .



There is dispersion (expected)

Starting position ($z = -7.0$ m) is (2,0)

At $z = 5.5$ m (\sim centre SSD) position varies with p_z within ~ 2 mm radius \rightarrow “4mm problem”

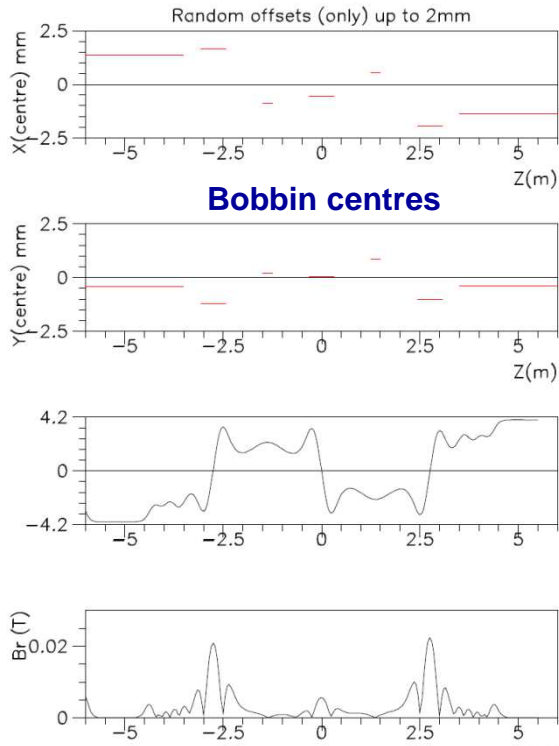
With 0.5 mm common offset problem becomes 1 mm

Not at all unexpected after a few moments thought.

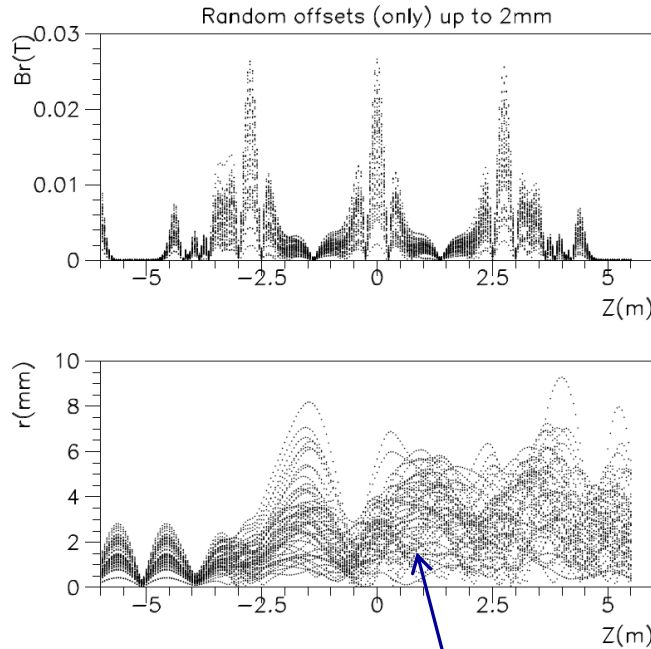
\rightarrow 2 mm is too much

Random offsets, no tilts

Shift bobbins randomly within $t = 2\text{mm}$ cylinders, no tilt



One set of offsets



Radial B

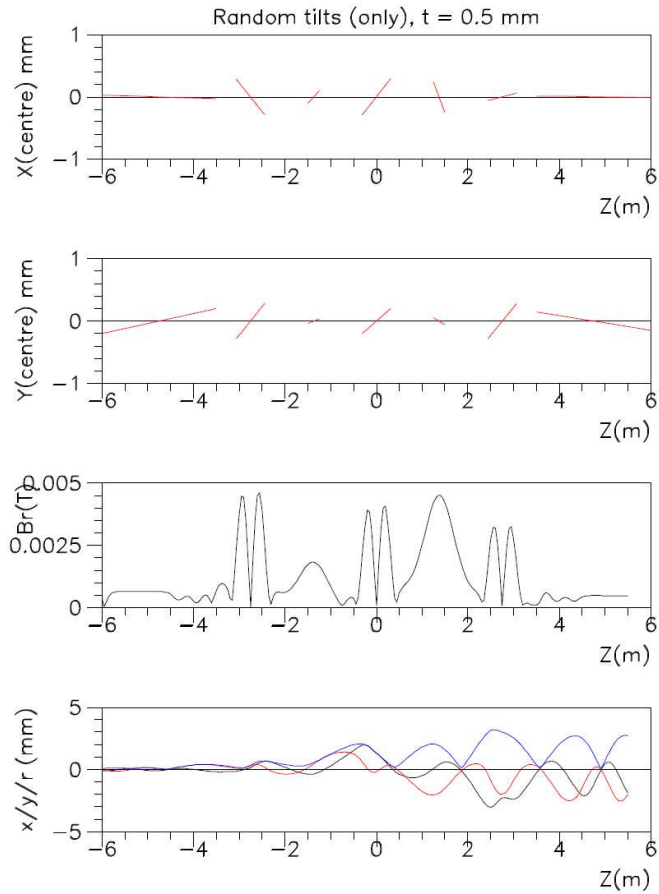
Radius (mm)

← Too much

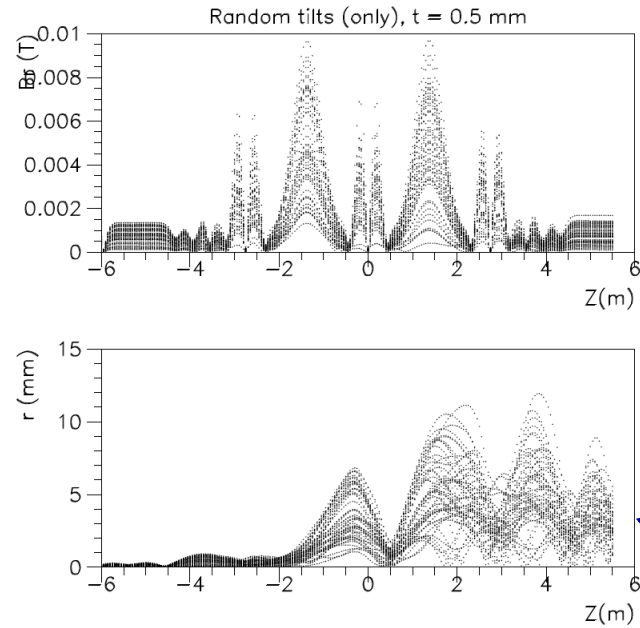
Reference trajectories for 50 random sets of offsets

Reducing t 0.5 mm reduces spread by ~ 4

Random tilts, no offsets, $t = 0.5$ mm



One set of tilts



Radial B

Radius (mm)

Too much

Reference trajectories for 50 random sets of tilts

TODAY'S CONCLUSION

Misalignment (tilt) of CC is big problem

Probably have to align axis of CC bobbin to $< 0.15\text{mm}$ at each end

Looking like $\sim 0.5\text{ mm}$ OK for FCs and SSs

Work in progress

Will be finished & documented in a few days